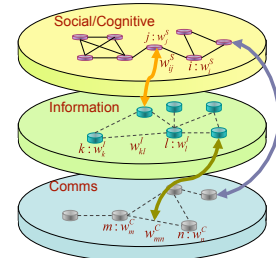


## Network Science

- A network is a collection of nodes, agents, ...
  - that collaborate to accomplish actions, gains, ...
  - that cannot be accomplished without such collaboration
- Network science
  - The Internet and other communication networks
  - Social networks
  - Biological networks
- Fundamental knowledge is necessary to design large, complex networks in such a way that their behaviors can be predicted prior to building them. (From National Research Council report on Network Science -- The National Academies Press, 2005)

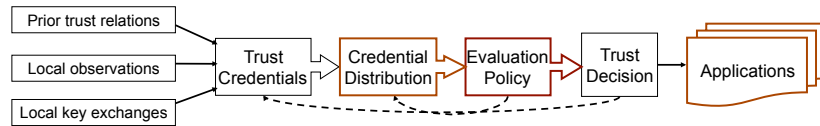
## Case study: Trust Management

- Multiple Interacting Graphs (Directed graphs)
  - Nodes**: agents, individuals, groups, organizations
  - Links**: ties, relationships
  - Weights on links**: value (strength, significance) of tie
  - Weights on nodes**: importance of node (agent)
- Value directed graphs with weighted nodes
- Real-life problems: **Dynamic, time varying graphs, relations, weights**



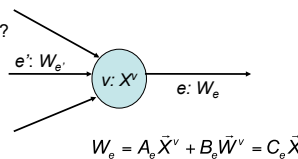
Organizational needs  
Network architecture and operation

- Objective: use mathematical analysis to understand and predict the emergent behaviors of distributed trust management systems in autonomic networks.



## Trust Credential Distribution

- No centralized trusted party; trust credentials are scattered in the network.
  - Where and how to find all needed credentials?
  - Where and how to store credentials such that searching is efficient?
- Network Coding Based Scheme
  - Extremely simple to implement
  - Only local information exchange
  - Easy for discovering new credentials
  - Efficient distribution



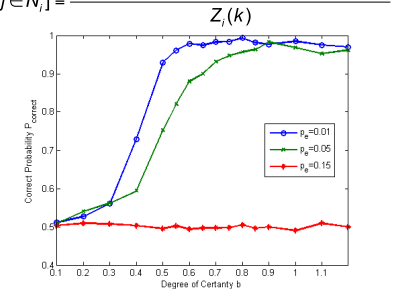
## Trust Evaluation Policy

- The trustworthiness of an agent is based on other peers' opinion
  - The most straightforward scheme is to ask neighbors to "vote" for it.
- Iterated stochastic voting:  $\Pr[s_i(k+1) | s_j(k), j \in \hat{N}_i] = \prod_{j \in \hat{N}_i} \Pr[d_{ij}, d_{ji} | s_j(k+1), s_j(k)] + \Pr[s_i(k+1)]$
- Convergence: unique stationary distribution.

Phase transitions in two parameters:

- Degree of certainty  $b$
- Probability of error  $p_e$

Theoretical analysis: results in the Ising model and the spin glass model, where  $d_{ij} = J_{ij}$ ; replica method.



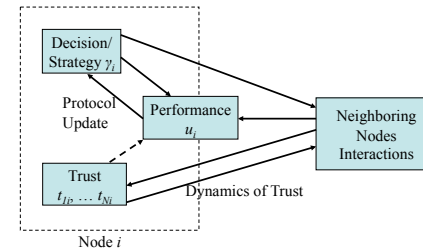
## Case study: Collaboration

- The nodes gain from collaborating
- But collaboration has costs (e.g. communications)
- Fundamental trade-off: gain from collaboration vs cost of collaboration

Constraint Coalitional Game

- Network formation game:
  - Payoff of node  $i$  from the network  $G$  is defined as  $v_i(G) = \text{gain} - \text{cost}$
  - Iterated process
    - Node pair  $ij$  is selected with probability  $p_{ij}$
    - If link  $ij$  is already in the network, the decision is whether to sever it, and otherwise the decision is whether to activate the link

## Trust and Collaboration



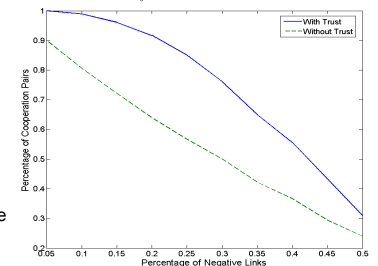
Two linked dynamics:

Trust propagation and game evolution

$$\gamma_i(k+1) = f^i(u_i(k), \gamma_i(k), \gamma_j(k), t_{ji}(k))$$

$$t_{ij}(k) = g^i(\gamma_j(k), t_{ij}(k-1), t_{ij}(k), v_{ji}^i(k)), \forall h \in N$$

$$u_i(k) = h^i(\gamma_i(k), \gamma_j(k))$$



Objective:

- to find what form or policy can induce all (or most) nodes to collaborate: maximize the coalition.

Two solutions:

- Negotiation: Players with positive gain can negotiate with their neighbors by sacrificing certain gain.
- Trust: By introducing a trust mechanism, all nodes are induced to collaborate without any negotiation.